

Fill Ups & Integer type Questions of Solutions

Fill in the Blanks

1. Given that ΔT_f is the depression in freezing point of the solvent in a solution of a non-volatile solute of molality, m , the quantity $\lim_{m \rightarrow 0} (\Delta T_f / m)$ is equal to

..... (1994 - 1 Mark)

Ans: K_f

Solutions : K_f ; Depression in freezing point, $\Delta T_f = K_f \cdot m$, where K_f is the molar depression constant or cryoscopy constant and m is the molality of the solution given by moles of solute per 1000 g of the solvent.

Integer Value Correct Type

1. 29.2% (w/w) HCl stock solution has a density of 1.25 g mL^{-1} . The molecular weight of HCl is 36.5 g mol^{-1} . The volume (mL) of stock solution required to prepare a 200 mL Solution of 0.4 M HCl is : (2012)

Ans : 8

Solution: Molarity of stock solution of HCl

$$= \frac{29.2 \times 1000 \times 1.25}{100 \times 36.5}$$

Let the volume of stock solution required = $V \text{ mL}$

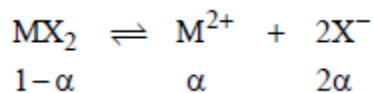
Thus
$$V \times \frac{29.2 \times 1000 \times 1.25}{100 \times 36.5} = 200 \times 0.4 = 8 \text{ mL}$$

2. MX_2 dissociates into M^{2+} and X^- ions in an aqueous solution, with a degree of dissociation (α) of 0.5. The ratio of the observed depression of freezing point of the aqueous solution to the value of the depression of freezing point in the absence of ionic dissociation is (JEE Adv. 2014)

Ans: 2



Solutions:



$$i = \frac{\text{obser. depression in f.pt of aq. solution}}{\text{depression of f.p.t. in absence of ionic dissociation}}$$

$$= \frac{1-\alpha+\alpha+2\alpha}{1} = 1+2\alpha = 1+2 \times 0.5 = 2$$

3. A compound H₂X with molar weight of 80g is dissolved in a solvent having density of 0.4 g ml⁻¹. Assuming no change in volume upon dissolution, the molality of a 3.2 molar solution is (JEE Adv. 2014)

Ans : 8

Solutions :
$$\text{Molality} = \frac{\text{wt. of solute in 1 L of solution} \times 1000}{\text{wt. of solvent in 1 L of solution} \times \text{mol wt. of solute}}$$

Calculation of wt. of solvent

$$1 \text{ mL of solvent} = 0.4 \text{ g}$$

$$1000 \text{ mL of solvent} = 400 \text{ g}$$

Calculation of wt. of solute

$$1000 \text{ mL of solution contain} = 3.2 \times 80 \text{ g solute} = 256 \text{ g}$$

$$\therefore \text{Molality} = \frac{256 \times 1000}{400 \times 80} = 8$$

4. If the freezing point of a 0.01 molar aqueous solution of a cobalt(III) chloride-ammonia complex (which behaves as a strong electrolyte) is -0.0558°C, the number of chloride(s) in the coordination sphere of the complex is [K_f of water = 1.86 K kg mol⁻¹] (JEE Adv. 2015)

Ans : 1

Solution :



Given $\Delta T_f = 0.0558^\circ\text{C}$

as we know, $\Delta T_f = i \times K_f \times m$

$$\Rightarrow 0.0558 = i \times 1.86 \times 0.01$$

$$i = 3$$

Therefore the complex will be $[\text{Co}(\text{NH}_3)_5\text{Cl}]\text{Cl}_2$

Hence number of chloride in co-ordination sphere is 1.

5. The mole fraction of a solute in a solution is 0.1. At 298 K, molarity of this solution is the same as its molality. Density of this solution at 298 K is 2.0 g cm^{-3} .

The ratio of the molecular weights of the solute and solvent, $\left(\frac{\text{MW}_{\text{solute}}}{\text{MW}_{\text{solvent}}}\right)$, is

Ans: 9

solution: 1 mole solution has 0.1 mole solute and 0.9 mole solvent.

Let M_1 = Molar mass solute

M_2 = Molar mass solvent

$$\text{Molality, } m = \frac{0.1}{0.9M_2} \times 1000 \quad \dots\dots(1)$$

$$\text{Molarity, } M = \frac{0.1}{0.1M_1 + 0.9M_2} \times 2 \times 1000 \quad \dots\dots(2)$$

$$\because m = M$$

$$\Rightarrow \frac{0.1 \times 1000}{0.9M_2} = \frac{200}{0.1M_1 + 0.9M_2}$$

$$\Rightarrow \frac{M_1}{M_2} = 9$$

Subjective Questions of Solutions, Past year Questions (Part - 1)

1. What is the molarity and molality of a 13% solution (by weight) of sulphuric acid with a density of 1.02 g/ml? To what volume should 100 ml of this acid be diluted in order to prepare a 1.5 N solution? (1978)

Ans : 1.38 M, 1.57 m, 184 ml

Solution :

$$\text{Molarity} = \frac{\text{Moles of solute}}{\text{Volume of solution in L}}$$

TIPS/Formulae : (i)

(ii) $N_1 V_1 = N_2 V_2$

A 13% solution (by weight) contains 13g of solute (i.e. H_2SO_4) per 100 gm of solution

$$\text{Moles of solute} = \frac{\text{Mass of } \text{H}_2\text{SO}_4}{\text{M. wt. of } \text{H}_2\text{SO}_4} = \frac{13}{98} = 0.1326$$

Volume of solution in L

$$= \frac{\text{Mass of solution}}{\text{density of solution} \times 1000} = \frac{100}{1.02 \times 1000} = 0.0980 \text{ Litre}$$

$$\therefore \text{Molarity of solution} = \frac{0.1326}{0.0980} = 1.35 \text{ M}$$

$$\text{Again, Molality} = \frac{\text{Moles of solute}}{\text{Mass of solvent in kg}}$$

Mass of solute in 100 ml of solution = 13 g [13 % solution]

Mass of solvent = Mass of solution – Mass of solute

$$= 100 - 13 = 87 \text{ g}$$

$$\therefore \text{Molality} = \frac{13/98}{87/1000} = 1.57 \text{ m}$$



$$\text{Normality} = \text{Molarity} \times \frac{\text{Mol. wt.}}{\text{Eq. wt.}} \text{ or } 1.35 \times \frac{98}{49} = 2.70 \text{ N}$$

$$\left[\begin{array}{l} \therefore \text{Eq. wt} = \frac{98}{2} \\ 2\text{H}_2\text{SO}_4 = 49 \end{array} \right]$$

$$N_1 = 2.70, V_1 = 100 \text{ ml}, N_2 = 1.5, V_2 = ?$$

$$N_1V_1 = N_2V_2; 2.70 \times 100 = 1.5 \times V_2$$

$$\text{or } V_2 = \frac{2.70 \times 100}{1.5} = 180 \text{ ml.}$$

\therefore 100 ml of this acid should be diluted to 180 ml to prepare 1.5 N solution

2. A bottle of commercial sulphuric acid (density 1.787 g/ml) is labelled as 86 percent by weight. What is the molarity of the acid. What volume of the acid has to be used to make 1 litre of 0.2 M H_2SO_4 ? (1979)

Ans: 15.81M; 12.65

Solution:

$$M = \frac{86/98}{100/1.787} \times 1000 = \frac{0.8775}{55.5} \times 1000 = 15.81 \text{ M}$$

$$M_1V_1 = M_2V_2$$

$$M_1 = 15.81, V_1 = ?$$

$$M_2 = 0.2, V_2 = 1 \text{ L} = 1000 \text{ ml}$$

$$\therefore 15.81 \times V_1 = 0.2 \times 1000$$

$$\text{or } V_1 = \frac{0.2 \times 1000}{15.81} = 12.65 \text{ ml}$$

\therefore Amount of acid to be used to make 1 L of 0.2 M $\text{H}_2\text{SO}_4 = 12.65$.



3. 0.5 gm of fuming H_2SO_4 (Oleum) is diluted with water. This solution is completely neutralized by 26.7 ml of 0.4 N NaOH. Find the percentage of free SO_3 in the sample of oleum. (1980)

Ans: 3.84%

Solution:

$$N_1 = 1, V_1 = ?, N_2 = 26.7, V_2 = 0.4$$

$$N_1 V_1 = N_2 V_2; 1 \times V_1 = 26.7 \times 0.4$$

$$V_1 = \frac{26.7 \times 0.4}{1} = 10.68$$

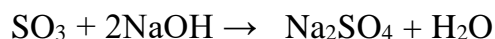
49g (Q eq wt of $\text{H}_2\text{SO}_4 = 49$) of H_2SO_4 will be neutralised by = 1N 1000 ml NaOH

\therefore 0.5g of H_2SO_4 will be neutralised by

$$= \frac{1000}{49} \times 0.5 = 10.20 \text{ ml } 1\text{N NaOH}$$

Volume of 1 N NaOH used by dissolved

$$\text{SO}_3 = 10.68 - 10.20 = 0.48 \text{ ml}$$



$$\therefore \text{Eq wt of } \text{SO}_3 = \frac{\text{Mol wt}}{2} = \frac{80}{2} = 40$$

Wt of SO_3 in 0.48 ml of 1 M solution

$$= \frac{40}{1000} \times 0.48 = 0.0192 \text{ g}$$

$$\% \text{ of } \text{SO}_3 = \frac{0.0192}{0.5} \times 100 = 3.84\%$$

4. The vapour pressure of pure benzene is 639.7 mm of mercury and the vapour of a solution of a solute in benzene at the same temperature is 631.9 mm of mercury. Calculate the molality of the solution. (1981 - 3 Marks)



Ans : 0.156 m/kg

Solution :

TIPS/Formulae : $\frac{P^{\circ} - P}{P^{\circ}} = \frac{n}{N}$ [Raoult's Equation]

Now the solution contains 'm' moles of solute per 1000 gm of benzene

Vapour pressure of benzene, $P^{\circ} = 639.7$ mm

Vapour pressure of solution, $P = 631.9$ mm

Moles of benzene (Mol. wt. 78), $N = 1000/78$

Moles of solute, $n = ?$

Substitute these values in the Raoult's equation

$$\frac{P^{\circ} - P}{P^{\circ}} = \frac{n}{N} \text{ or } \frac{639.7 - 631.9}{639.7} = \frac{n \times 78}{1000}$$

$$\text{or } \frac{7.8}{639.7} = \frac{78n}{1000} \quad \therefore n = \frac{1000 \times 7.8}{78 \times 639.7} = 0.156$$

Hence, molality of solution = 0.156 m

5. An organic compound $C_xH_{2y}O_y$ was burnt with twice the amount of oxygen needed for complete combustion to CO_2 and H_2O . The hot gases when cooled to $0^{\circ}C$ and 1 atm. pressure, measured 2.24 liters. The water collected during cooling weighed 0.9 g. The vapour pressure of pure water at $20^{\circ}C$ is 17.5 mm Hg and is lowered by 0.104 mm when 50 g of the organic compound are dissolved in 1000 g of water. Give the molecular formula of the organic compound. (1983 - 5 Marks)

Ans: $(CH_2O)_5$ or $C_5H_{10}O_5$

Solution: The chemical equation for the combustion of organic compound $C_xH_{2y}O_y$ can be represented as:



The gases obtained after cooling = $x + x = 2x$

$\therefore 2x = 2.24$ litres [\because H₂O is in liquid state]

$$\text{or } x = \frac{2.24}{2} = 1.12 \text{ litres}$$

Number of moles of CO₂ =

$$\frac{1.12 \text{ litres}}{22.4 \text{ litres mole}}$$

[\because 22.4 L at NTP = 1 mole]

$$= \frac{1}{20} \text{ mole} = 0.05 \text{ mole}$$

The empirical formula of the organic compound is C(H₂O) ... (1)

The mole fraction of the solute (A)

= relative decrease in vapour pressure of the solvent (B)

$$\frac{p^\circ - p}{p^\circ} = \frac{\frac{W_A}{M_A}}{\frac{W_A}{M_A} + \frac{W_B}{M_B}}$$

$$\text{or } \frac{0.104}{17.5} = \frac{\frac{50}{M_A}}{\frac{50}{M_A} + \frac{1000}{18}} \quad [M_A = \text{mol. wt. g A}]$$

$$\text{or } \frac{0.104}{17.5} = \frac{50}{M_A \left(\frac{50 \times 18 + 1000M_A}{18M_A} \right)}$$

$$\text{or } \frac{104}{17500} = \frac{50 \times 18}{900 + 1000M_A} \quad \text{or } M_A = 150.6$$

Molecular wt. of the organic compound



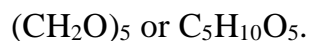
$$(\text{CH}_2\text{O})_n = 150$$

$$\text{Molecular wt. of CH}_2\text{O} = 12 + 2 + 16 = 30$$

$$\therefore 30 \times n = 150 \quad [\because (\text{CH}_2\text{O})_n = \text{mol. formula}]$$

$$\text{or } n = 150/30 = 5$$

\therefore Molecular formula of the given organic compound is



6. 'Two volatile and miscible liquids can be separated by fractional distillation into pure component', is true under what conditions? (1984 - 1 Mark)

Solution: If they form an ideal solution which obeys' Raoult's Law and for which $\Delta H_{\text{mixing}} = 0$ and $\Delta V_{\text{mixing}} = 0$

Thus we can separate two volatile and miscible liquids by fractional distillation if, they should not form a zeotropic solutions.



Subjective Questions of Solutions, Past year Questions (Part - 2)

7. The vapour pressure of ethanol and methanol are 44.5 mm and 88.7 Hg respectively. An ideal solution is formed at the same temperature by mixing 60 g of ethanol with 40 g of methanol. Calculate the total vapour pressure of the solution and the mole fraction of methanol in the vapour. (1986 - 4 Marks)

Ans : 66.17 mm, 0.65

Solution :

TIPS/Formulae :

$$P_{\text{total}} = p_A + p_B$$

$$\text{Molecular weight of CH}_3\text{OH} = 12 + 3 + 16 + 1 = 32$$

$$\text{Molecular weight of C}_2\text{H}_5\text{OH} = 24 + 5 + 16 + 1 = 46$$

According to Raoult's law

$$P_{\text{total}} = p_1 + p_2$$

where P_{total} = Total vapour pressure of the solution

p_1 = Partial vapour pressure of one component

p_2 = Partial vapour pressure of other component

Again, $p_1 = \text{Vapour pressure } (p_1^\circ) \times \text{mole fraction}$

Similarly, $p_2 = \text{Vapour pressure } (p_2^\circ) \times \text{mole fraction}$

$$\text{Mole fraction of CH}_3\text{OH} = \frac{\frac{40}{32}}{\frac{40}{32} + \frac{60}{46}} = 0.49$$



$$\frac{\frac{60}{46}}{\frac{60}{46} + \frac{40}{32}} = 0.51$$

Mole fraction of ethanol =

NOTE THIS STEP: Thus now let us first calculate the partial vapour pressures, i.e., p_1 and p_2 of the two component.

Partial vapour pressure of CH_3OH (p_1) = $88.7 \times 0.49 = 43.48$ mm

Partial vapour pressure of $\text{C}_2\text{H}_5\text{OH}$ (p_2) = $44.5 \times 0.51 = 22.69$ mm

\therefore Total vapour pressure of the solution = $43.48 + 22.69$ mm = 66.17 mm

Mole fraction of CH_3OH in vapour = $\frac{43.48}{66.17} = 0.65$

8. The vapour pressure of a dilute aqueous solution of glucose ($\text{C}_6\text{H}_{12}\text{O}_6$) is 750 mm of mercury at 373 K. Calculate (i) molality and (ii) mole fraction of the solution. (1989 - 3 Marks)

Ans: 0.7503 mol/kg, 0.9868

Solution:

TIPS/Formulae:

$$\text{Molality, } M = \frac{\text{moles of solute}}{\text{kg of solvent}}$$

$$\text{Mole fraction, } x_A = \frac{n_A}{n_A + n_B}, \quad x_B = \frac{n_B}{n_A + n_B}$$

$$p_1 = x_1 p_1^\circ$$

$$\therefore x_1 = \frac{p_1}{p_1^\circ} = \frac{750}{760} = 0.9868$$

$$x_2 (\text{solute}) = 1 - 0.9868 = 0.0132$$



$$\text{Molality, } m = \frac{x_2}{x_1 M_1} \times 1000 = \frac{0.0132 \times 1000}{0.9868 \times 18}$$

$$= 0.7503 \text{ mol kg}^{-1}$$

9. The vapour pressure of pure benzene at a certain temperature is 640 mm Hg. A non-volatile non-electrolyte solid weighing 2.175 g is added to 39.0 g of benzene. The vapour pressure of the solution is 600 mm Hg. What is the molecular weight of the solid substance? (1990 - 3 Marks)

Ans: 65.25

Solution:

TIPS/Formulae:

According to Raoult's law,

$$\frac{p^\circ - p}{p^\circ} = \frac{w/m}{w/m + W/M}$$

Here, $p^\circ = 640 \text{ mm}$

$p = 600 \text{ mm}$

$w = 2.175 \text{ g}$

$= 39.0$

$m = ?$

$M = 78$

Substituting the various values in the above equation for Raoult's law:

$$\frac{640 - 600}{640} = \frac{2.175/m}{2.175/m + 39/78}$$

$$\frac{1}{16} = \frac{2.175}{2.175 + 0.5m} \Rightarrow m = 65.25$$



10. The degree of dissociation of calcium nitrate in a dilute aqueous solution, containing 7.0 g. of the salt per 100 gm of water at 100°C is 70%. If the vapour pressure of water at 100°C is 760 mm, calculate the vapour pressure of the solution. (1991 - 4 Marks)

Ans : 746.3 mm Hg

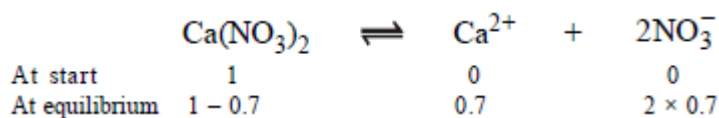
Solution :

TIPS/Formulae : First find moles of $\text{Ca}(\text{NO}_3)_2$ and water.

Then use the expression $\frac{p^\circ - p}{p^\circ} = \frac{n}{n + N}$ to find vapour pressure of solution.
Let initially 1 mole of $\text{Ca}(\text{NO}_3)_2$ is taken

Degree of dissociation of $\text{Ca}(\text{NO}_3)_2 = 70/100 = 0.7$

Ionisation of $\text{Ca}(\text{NO}_3)_2$ can be represented as



\therefore Total number of moles in the solution at equilibrium = $(1 - 0.7) + 0.7 + 2 \times 0.7 = 2.4$

No. of moles when the solution contains 1 gm of calcium nitrate instead of 1 mole of the salt

$$n = \frac{2.4}{164} \times 7 = 0.102$$

$$\frac{\text{Wt. of water}}{\text{Mol. wt. of water}} = \frac{100}{18} = 5.55$$

Applying Raoult's law, $\frac{p^\circ - p}{p^\circ} = \frac{n}{n + N}$

$$\frac{760 - p}{760} = \frac{0.102}{0.102 + 5.55} \Rightarrow \frac{760 - p}{760} = 0.0180$$

$$\Rightarrow p = 760 - (760 \times 0.0180) = 746.3 \text{ mm Hg}$$

11. Addition of 0.643 g of a compound to 50 ml. of benzene (density : 0.879 g/ml.) lowers the freezing point from 5.51°C to 5.03°C. If K_f for benzene is 5.12 K kg mol⁻¹, calculate the molecular weight of the compound. (1992 - 2 Marks)

Ans : 156.056

Solution :

TIPS/Formulae :

Given Wt. of benzene (solvent),

$$W = \text{Volume} \times \text{density} = 50 \times 0.879 = 43.95 \text{ g}$$

Wt. of compound (solute), $w = 0.643 \text{ g}$

Mol. wt. of benzene, $M = 78$; Mol. wt. of solute, $m = ?$

Depression in freezing point, $\Delta T_f = 5.51 - 5.03 = 0.48$

Molar freezing constant, $K_f = 5.12$

Now we know that,

$$m = \frac{1000 \times K_f \times w}{W \times \Delta T_f} = \frac{1000 \times 5.12 \times 0.643}{43.95 \times 0.48} = 156.056$$

12. What weight of the non-volatile solute, urea ($\text{NH}_2 - \text{CO} - \text{NH}_2$) needs to be dissolved in 100g of water, in order to decrease the vapour pressure of water by 25%? What will be the molality of the solution? (1993 - 3 Marks)

Ans : 18.52 m

Solution :

TIPS/Formulae :



$$\frac{p^\circ - p}{p^\circ} = \frac{\frac{w}{m}}{\frac{w}{m} + \frac{W}{M}}$$

Here, w and m are wt. and molecular wt. of solute, W and M are wt. and molecular weight of solvent

p = Pressure of solution; p° = Normal vapour pressure

Let the initial (normal) pressure (p°) = p

$$\therefore \text{Pressure of solution} = \frac{75}{100} \times p = \frac{3}{4} p$$

m = 60, M = 18, W = 100 gm

$$\therefore \frac{p - \frac{3}{4}p}{p} = \frac{\frac{w}{60}}{\frac{w}{60} + \frac{100}{18}} \Rightarrow \frac{1}{4} = \frac{w/60}{(w/60) + 5.55}$$

$$\frac{4w}{60} = \frac{w}{60} + 5.55 \Rightarrow \frac{3w}{60} = \frac{w}{20} = 5.55 \text{ or } w = \mathbf{111 \text{ g}}$$

$$\begin{aligned} \text{Molality} &= \frac{\text{No. of moles of solute}}{\text{Wt. of solvent}} \times 1000 \\ &= \frac{111 \times 1000}{60 \times 100} = \mathbf{18.52 \text{ m}} \end{aligned}$$

13. The molar volume of liquid benzene (density=0.877 g mL⁻¹) increases by a factor of 2750 as it vaporises at 20°C and that of liquid toluene (density=0.867 g mL⁻¹) increases by a factor of 7720 at 20°C. A solution of benzene and toluene at 20°C has a vapour pressure of 46.0 Torr. Find the mole fraction of benzene in the vapour above the solution. (1996 - 3 Marks)

Ans : 0.73



Solution :

TIPS/Formulae :

$$(i) \text{ Volume} = \frac{\text{No. of moles} \times \text{molar mass}}{\text{density}}$$

$$(ii) PV = nRT \text{ or } P = \frac{nRT}{V}$$

Volume of 1 mole of liq. benzene = $78/0.877$

Volume of 1 mole of toluene = $92/0.867$

In vapour phase,

At 20°C , for 1 mole of benzene,

$$\text{Volume} = \frac{1 \times 78 \times 2750}{0.877} = 244583.80 \text{ mL} = 244.58 \text{ L}$$

Similarly for 1 mole of toluene,

$$\text{volume} = \frac{1 \times 92}{0.867} \times 7720 = 819192.61 \text{ mL} = 819.19 \text{ L}$$

As we know that, $PV = nRT$

$$\text{For benzene, } P_B^o = \frac{nRT}{V} = \frac{1 \times 0.0821 \times 293}{244.58} \text{ atm} = 0.098 \text{ atm}$$

$$\text{For toluene, } P_T^o = \frac{nRT}{V} = \frac{1 \times 0.0825 \times 293}{819.19} \text{ atm} = 0.029 \text{ atm}$$

$$P = P_B^o X_B + P_T^o X_T$$

$$\because X_B + X_T = 1 \quad \therefore X_T = 1 - X_B$$

$$P = P_B^o X_B + P_T^o (1 - X_B)$$

Total vapour-pressure = $46 \text{ torr} = 46/760 = 0.060 \text{ atm}$



$$\text{Thus, } 0.060 = 0.098 X_B + 0.029 (1 - X_B)$$

$$\Rightarrow 0.060 = 0.098 X_B + 0.029 - 0.029 X_B$$

$$\Rightarrow 0.031 = 0.069 X_B$$

$$\therefore X_B = \frac{0.031}{0.069} = 0.45 \text{ (in liquid phase)}$$

$$X_B + X_T = 1$$

$$X_T = 1 - 0.45 = 0.55 \text{ (in liquid phase)}$$

$$\text{Also, } P_B' = P_B^o X_B = P X_B'$$

$$\text{So, } 0.098 \times 0.45 = 0.060 \times X_B'$$

$$X_B' = \frac{0.098 \times 0.45}{0.060} = 0.735 \text{ (in gas phase)}$$



Subjective Questions of Solutions, Past year Questions (Part - 3)

14. A solution of a nonvolatile solute in water freezes at -0.30°C . The vapour pressure of pure water at 298 K is 23.51 mm Hg and K_f for water is $1.86 \text{ K kg mol}^{-1}$. Calculate the vapour pressure of this solution at 298 K. (1998 - 4 Marks)

Ans: 23.44 mm Hg

Solution:

TIPS/Formulae:

$$\Delta T_f = K_f \cdot m$$

$$\frac{P^{\circ} - p}{p^{\circ}} = \frac{\text{moles of solute}}{\text{moles of solvent}}$$

Depression in freezing point, $\Delta T_f = 0 - (-0.30) = 0.30$

Now we know that $\Delta T_f = K_f m$

$$\therefore m = \frac{\Delta T_f}{K_f} = \frac{0.30}{1.86} = 0.161$$

According to Raoult's law

$$\frac{p^{\circ} - p}{p^{\circ}} = \frac{\text{No. of moles of solute}}{\text{No. of moles of solvent}}$$

$$\frac{23.51 - p}{23.51} = \frac{0.161}{1000/18} = \frac{0.161 \times 18}{1000}$$

(\because No. of moles of $\text{H}_2\text{O} = 1000/18$)

On usual calculations

$$\frac{23.51 - p}{23.51} = .0020898$$



$$p = 23.51 - 23.51 \times 0.0020898 = 23.51 - .068$$

$$p = 23.44 \text{ mm Hg}$$

15. Nitrobenzene is formed as the major product along with a minor product in the reaction of benzene with a hot mixture of nitric acid and sulphuric acid. The minor product consists of carbon: 42.86%, hydrogen: 2.40%, nitrogen : 16.67%, and oxygen: 38.07% (i) Calculate the empirical formula of the minor product. (ii) When 5.5 g of the minor product is dissolved in 45 g of benzene, the boiling point of the solution is 1.84 °C higher than that of pure benzene. Calculate the molar mass of the minor product and determine its molecular and structural formula. (Molar boiling point elevation constant of benzene is 2.53 K kg mol⁻¹.) (1999 - 10 Marks)

Ans : 168 g, C₆H₄ (NO₂)₂, m-dinitrobenzene

Solution :

TIPS/Formulae : $\Delta T_b = k_b \cdot m$

Element	%	Relative no. of atoms	Simplest ratio
C	42.86	$\frac{42.86}{12} = 3.57$	$\frac{3.57}{1.19} = 3$
H	2.40	$\frac{2.40}{1} = 2.40$	$\frac{2.40}{1.19} = 2$
N	16.67	$\frac{16.67}{14} = 1.19$	$\frac{1.19}{1.19} = 1$
O	38.07	$\frac{38.07}{16} = 2.38$	$\frac{2.38}{1.19} = 2$

∴ Empirical formula of the minor product is C₃H₂NO₂ Molar empirical formula mass of the minor product = 3 × 12 + 2 × 1 + 1 × 14 + 2 × 16 = 84 g mol⁻²

Let M be the molar mass of the minor product. For 5.5 g of the minor product dissolved in 45 g benzene, the molality

$$(m) \text{ of the solution} = \frac{5.5 \text{ g/M}}{0.045 \text{ kg}}$$

Substituting this in the expression of elevation of boiling point,



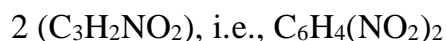
$$\Delta T_b = K_b m \Rightarrow 1.84\text{K} = (2.53 \text{ Kmol}^{-1}) \left(\frac{5.5\text{g/M}}{0.045\text{kg}} \right)$$

$$\text{or } M = 168 \text{ g mol}^{-1}$$

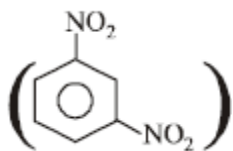
No. of unit of empirical formula in molecular formula

$$= \frac{168 \text{ g mol}^{-1}}{84 \text{ g F}} = 2$$

Hence the molecular formula of the minor product is



The product is m - dinitrobenzene .



16. To 500 cm³ of water, 3.0 × 10⁻³ kg of acetic acid is added. If 23% of acetic acid is dissociated, what will be the depression in freezing point? K_f and density of water are 1.86 K kg⁻¹ mol⁻¹ and 0.997 g cm⁻³, respectively. (2000 - 3 Marks)

Ans : 0.228 K

Solution :

TIPS/Formulae :

$$\Delta T_f = i x K_f x m$$

$$\text{Weight of water} = 500 \times 0.997 = 498.5 \text{ g}$$

(weight = volume × density)

No. of moles of acetic acid

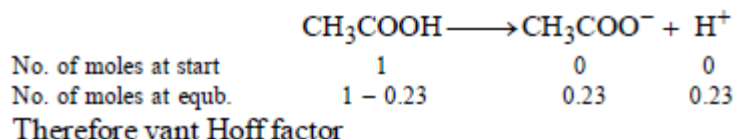
$$= \frac{\text{Wt. of CH}_3\text{COOH in g}}{\text{Mol. wt. of CH}_3\text{COOH}} = \frac{3 \times 10^{-3} \times 10^3}{60} = 0.05$$

Since 498.5 g of water has 0.05 moles of CH_3COOH

$$1000 \text{ g of water has} = \frac{0.05 \times 1000}{498.5} = 0.1$$

Therefore molality of the solution = 0.1

Determination of van't Hoff factor, i



$$\begin{aligned} &= \frac{\text{No. of particles before dissociation}}{\text{No. of particles after dissociation}} \\ &= \frac{1 - 0.23 + 0.23 + 0.23}{1} = 1.23 \end{aligned}$$

Now we know that

$$\Delta T_f = i \times K_f \times m = 1.23 \times 1.86 \times 0.1 = 0.228\text{K}$$

17. 1.22g of benzoic acid is dissolved in 100 g of acetone and 100 g of benzene separately. Boiling point of the solution in acetone increases by 0.17°C , while that in the benzene increases by 0.13°C ; K_b for acetone and benzene is $1.7 \text{ K kg mol}^{-1}$ and $2.6 \text{ K kg mol}^{-1}$. Find molecular weight of benzoic acid in two cases and justify your answer. (2004 - 2 Marks)

Ans : 122, 224

Solution :

TIPS/Formulae :

$$\Delta T_b = K_b \times M$$

In first case,



$$\Delta T_b = K_b \times m = K_b \times \frac{\text{Wt. of solute}}{\text{Mol. wt. of solute}}$$

$$\text{or } 0.17 = 1.7 \times \frac{1.22}{M \times 100 \times 10^{-3}} \text{ or } M = 122$$

Thus the benzoic acid exists as a monomer in acetone

(ii) In second case,

$$\Delta T_b = K_b \times \frac{\text{Wt. of solute}}{\text{Mol. wt. of solute}}$$

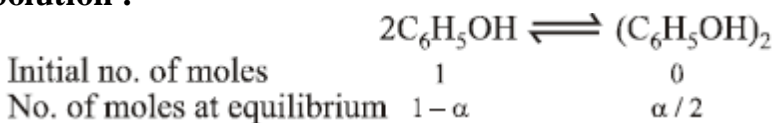
$$\text{or } 0.13 = 2.6 \times \frac{1.22}{M' \times 100 \times 10^{-3}} \Rightarrow M' = 224$$

NOTE : Double the expected molecular weight of benzoic acid (244) in acetone solution indicates that benzoic acid exists as a dimer in acetone.

18. 75.2 g of C₆H₅OH (phenol) is dissolved in a solvent of K_f = 14. If the depression in freezing point is 7 K then find the % of phenol that dimerises. (2006 - 6M)

Ans : 75%

Solution :



$$\text{Total number of moles at equilibrium} = 1 - \alpha + \frac{\alpha}{2} = 1 - \frac{\alpha}{2}$$

$$\Delta T_f = iK_f \times (\text{molality})$$

$$\Rightarrow 7 = 14 \times \frac{75.2}{94} \times \left(1 - \frac{\alpha}{2}\right) \left[\begin{array}{l} \text{weight of phenol} = 75.2\text{g} \\ \text{mol.wt of phenol} = 94 \end{array} \right]$$

$\therefore a = 0.75$ So the percentage of phenol that dimerises = 75%.

